

B 2.2

Kosinus-Satz im Dreieck AED:

$$\overline{ED}^2 = \overline{AE}^2 + \overline{AD}^2 - 2 \cdot \overline{AE} \cdot \overline{AD} \cdot \cos \sphericalangle BAD$$

$$\Leftrightarrow \overline{ED}^2 = [(60 - 10)^2 + 40^2 - 2 \cdot (60 - 10) \cdot 40 \cdot \cos 60^\circ] \text{ m}^2$$

$$\Leftrightarrow \overline{ED}^2 = 2100 \text{ m}^2$$

$$\Leftrightarrow \overline{ED} = 45,83 \text{ m}$$

B 2.3

$$A_{\text{blau}} = \overline{EB} \cdot \overline{HD} = 10 \text{ m} \cdot 34,64 \text{ m} = 346,40 \text{ m}^2$$

B 2.4

$$\sphericalangle BAC = \sphericalangle DCA = 36,67^\circ$$

Kosinus-Satz im Dreieck ABC:

$$\overline{BC}^2 = \overline{AB}^2 + \overline{AC}^2 - 2 \cdot \overline{AB} \cdot \overline{AC} \cdot \cos \sphericalangle BAC$$

$$\Leftrightarrow \overline{BC}^2 = [60^2 + 58^2 - 2 \cdot 60 \cdot 58 \cdot \cos 36,67^\circ] \text{ m}^2$$

$$\Leftrightarrow \overline{BC}^2 = 1381,46 \text{ m}^2$$

$$\Leftrightarrow \overline{BC} = 37,17 \text{ m}$$

Sinus-Satz im Dreieck ABC:

$$\frac{\overline{BC}}{\sin \sphericalangle BAC} = \frac{\overline{AB}}{\sin \sphericalangle ACB}$$

$$\Leftrightarrow \sin \sphericalangle ACB = \frac{\sin \sphericalangle BAC \cdot \overline{AB}}{\overline{BC}}$$

$$\Leftrightarrow \sin \sphericalangle ACB = \frac{\sin 36,67^\circ \cdot 60}{37,17} = 0,96$$

$$\Leftrightarrow \sphericalangle ACB = 74,58^\circ$$

B 2.5

$$\sphericalangle CAD = 180^\circ - \sphericalangle ADC - \sphericalangle DCA = 180^\circ - 120^\circ - 36,67^\circ = 23,33^\circ$$

Sinus-Satz im Dreieck ACD:

$$\frac{\overline{DC}}{\sin \sphericalangle CAD} = \frac{\overline{AC}}{\sin \sphericalangle ADC}$$

$$\Leftrightarrow \overline{DC} = \frac{\overline{AC} \cdot \sin \sphericalangle CAD}{\sin \sphericalangle ADC} \text{ m}$$

$$\Leftrightarrow \overline{DC} = \frac{58 \cdot \sin 23,33^\circ}{\sin 120^\circ} \text{ m} = 26,52 \text{ m}$$

$$\overline{CF} = \overline{DC} - \overline{EB} = 26,52 \text{ m} - 10 \text{ m} = 16,52 \text{ m}$$

$$A_{\text{Sektor}} = \overline{CF}^2 \cdot \pi \cdot \frac{360^\circ - (\sphericalangle ACB + \sphericalangle DCA)}{360^\circ} \text{ m}^2$$

$$\Leftrightarrow A_{\text{Sektor}} = 16,52^2 \cdot \pi \cdot \frac{360^\circ - 74,58^\circ - 36,67^\circ}{360^\circ} \text{ m}^2 = 592,42 \text{ m}^2$$

B 2.6

$$A_{\text{blau}} = 346,40 \text{ m}^2$$

$$A_{\text{Trapez}} = 0,5 \cdot (\overline{DC} + \overline{AB}) \cdot \overline{HD}$$

$$\Leftrightarrow A_{\text{Trapez}} = 0,5 \cdot (26,52 + 60) \cdot 34,64 \text{ m}^2 = 1498,53 \text{ m}^2$$

$$A_{\text{alles}} = 1498,53 \text{ m}^2 + 592,42 \text{ m}^2 = 2090,95 \text{ m}^2$$

$$(592,42 + 346,40) : 2090,95 = 0,4490 \Rightarrow 44,90 \%$$